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antilog antilogarithm (\log^{-1})	89	$E_n(z)$ exponential integral	228
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Notation — Greek Letters

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$B(z, w)$ beta function.....	258	$\Lambda_0(\varphi \alpha)$ Heuman's lambda function.....	595
γ Euler's constant.....	255	$\mu(f_n)$ mean difference.....	877
$\gamma(a, x)$ incomplete gamma function (normalized).....	260	$\mu(n)$ Möbius function.....	826
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Miscellaneous Notations

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i ($=\sqrt{-1}$).....	70	Σ overall summation.....	822
$\binom{n}{k}$ binomial coefficient.....	10	Σ' restricted summation.....	755
$n!$ factorial function.....	255	$\Sigma \Pi$ sum or product taken over all prime numbers p	807
$(2n)!! = 2 \cdot 4 \cdot 6 \dots (2n) = 2^n n!$	258	$\sum_{d n} \prod_{d n} \Pi$ sum or product overall positive divisors d of n	826
(m, n) greatest common divisor.....	822	\int Cauchy's principal value of the integral.....	228
$(n, k) = \frac{\Gamma(\frac{1}{2}+n+k)}{k! \Gamma(\frac{1}{2}+n-k)}$ (Hankel's symbol).....	437	\approx approximately equal.....	14
$(n; n_1, n_2, \dots, n_m)$ multinomial coefficient.....	823	\sim asymptotically equal.....	15
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		\neq unequal.....	12